# Radar Systems Engineering Lecture 7 Part 2 Radar Cross Section 

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## Methods of Radar Cross Section Calculation

| RCS Method | Approach to Determine <br> Surface Currents |
| :---: | :---: |
| Finite Difference- | Solve Differential Form of Maxwell's <br> Equation's for Exact Fields |
| Method of Moments <br> (MoM) | Solve Integral Form of Maxwell's <br> Equation's for Exact Currents |
| Physical Optics <br> (PO) | Currents Approximated by Tangent <br> Plane Method |
| Physical Theory of <br> Diffraction (PTD) | Physical Optics with Added Edge <br> Current Contribution |
| Geometrical Optics <br> (GO) | Current Contribution Assumed to Vanish <br> Except at Isolated Specular Points |
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## Electromagnetic Scattering



- Two step process to determine scattered fields
- Determine induced surface currents
- Calculate field radiated by currents


## Method of Moments (MoM) Overview

- The Method of Moments calculations predict the exact solution for the target RCS
- Method - Solve integral form of Maxwell's Equations
- Generate a surface patch model for the target
- Transform the integral equation form of Maxwell's equations into a set of homogeneous linear equations
- The solution gives the surface current densities on the target
- The scattered electric field can then be calculated in a straight forward manner from these current densities
- Knowledge of the scattered electric field then allows one to readily calculate the radar cross section
- Significant limitations of this method
- Inversion of the matrix to solve the homogeneous linear equations
- Matrix size can be very large at high frequencies

Patch size typically $\sim \lambda / 10$

## Standard Spherical Coordinate System



## Spherical Coordinate System for MOM Calculations

- Source currents distributed over surface $\mathbf{S}^{\prime}$
- Field observation point located at ( $x, y, z$ )
- Point on surface $S^{\prime}$ is $\left(x^{\prime}, y^{\prime}, z^{\prime}\right)$



## Method of Moments

- Maxwell's Equations transform to the Stratton and Chu Equations using the vector Green's Theorem and yield:

$$
\begin{aligned}
& \overrightarrow{\mathbf{E}}_{\mathrm{S}}=\oiint_{S^{\prime}}[+\mathbf{i} \omega \mu(\hat{\mathbf{n}} \times \overrightarrow{\mathbf{H}}) \psi+(\hat{\mathbf{n}} \times \overrightarrow{\mathbf{E}}) \mathbf{x} \vec{\nabla} \psi+(\hat{\mathbf{n}} \cdot \overrightarrow{\mathbf{E}}) \vec{\nabla} \psi] \mathbf{d S}^{\prime} \\
& \overrightarrow{\mathbf{H}}_{\mathrm{S}}=\oiint_{S^{\prime}}[+\mathbf{i} \omega \varepsilon(\hat{\mathbf{n}} \times \overrightarrow{\mathbf{E}}) \psi-(\hat{\mathbf{n}} \times \overrightarrow{\mathbf{H}}) \mathbf{x} \vec{\nabla} \psi-(\hat{\mathbf{n}} \cdot \overrightarrow{\mathbf{H}}) \vec{\nabla} \psi] \mathrm{dS}^{\prime} \\
& \psi=\left[\frac{\mathbf{e}^{+i k R}}{4 \pi \mathbf{R}}\right]=\begin{array}{c}
\text { Free Space } \\
\text { Green's Function }
\end{array} \quad \mathbf{R}=\left|\mathbf{r}-\mathbf{r}^{\prime}\right|
\end{aligned}
$$

- Free space Green's function is an spherical wave falling of as: $1 / R$
- Also, note: $\overrightarrow{\mathbf{E}}=\overrightarrow{\mathbf{E}}_{\mathrm{I}}+\overrightarrow{\mathbf{E}}_{\text {S }}$

$$
\overrightarrow{\mathbf{H}}=\overrightarrow{\mathbf{H}}_{\mathrm{I}}+\overrightarrow{\mathbf{H}}_{\mathrm{S}}
$$

## Method of Moments (continued once)

- On the surface of the perfectly conducting target these equations become:
- Total tangential electric field zero at surface
- No magnetic sources of currents or charges as source of scattered fields
- Electric Field Integral Equation (EFIE)

$$
\overrightarrow{\mathbf{E}}_{\mathrm{S}}=\oiint_{S^{\prime}}[+\mathbf{i} \omega \mu(\hat{\mathbf{n}} \mathbf{x} \overrightarrow{\mathbf{H}}) \psi+(\hat{\mathbf{n}} \cdot \overrightarrow{\mathbf{E}}) \nabla \psi] \mathrm{dS}^{\prime}=\oiint_{\mathbf{S}^{\prime}}\left[+\mathbf{i} \omega \mu \mathbf{J} \psi+\frac{\mathbf{1}}{\varepsilon} \rho \nabla \psi\right] \mathbf{d S}^{\prime}
$$

- Magnetic Field Integral Equation (MFIE)

$$
\overrightarrow{\mathbf{H}}_{\mathrm{S}}=\oiint_{\mathrm{S}^{\prime}}(\hat{\mathbf{n}} \mathbf{x} \overrightarrow{\mathbf{H}}) \mathbf{x} \nabla \psi \mathbf{d} \mathbf{S}^{\prime}=\oint_{\mathrm{S}^{\prime}} \overrightarrow{\mathbf{J}} \mathbf{x} \nabla \psi \mathbf{d} \mathbf{S}^{\prime}
$$

- Causes of scattered fields
- Scattered electric field - electric currents and charges
- Scattered magnetic field - electric currents


## Method of Moments (continued twice)

- Applying the boundary conditions for Maxwell's Equations and the Continuity Equation to free space yields:

$$
\begin{aligned}
& \hat{\mathbf{n}} \times \overrightarrow{\mathbf{E}}_{\mathrm{I}}=-\hat{\mathbf{n}} \mathbf{x} \overrightarrow{\mathbf{E}}_{\mathrm{S}}=\hat{\mathbf{n}} \mathbf{x} \oiint_{\mathbf{S}^{\prime}}\left[+\mathbf{i} \omega \mu \overrightarrow{\mathbf{J}} \psi+\frac{+\mathbf{i}}{\omega \varepsilon} \nabla \cdot \overrightarrow{\mathbf{J}} \nabla \psi\right] \mathbf{d S}^{\prime} \\
& \hat{\mathbf{n}} \mathbf{x} \overrightarrow{\mathbf{H}}_{\mathrm{I}}=\frac{\overrightarrow{\mathbf{J}}}{\mathbf{2}}-\hat{\mathbf{n}} \mathbf{x} \oiint_{\mathrm{S}^{\prime}} \overrightarrow{\mathbf{J}} \mathbf{x} \nabla \psi \mathbf{d S}^{\prime}
\end{aligned}
$$

- Procedure to calculate the scattered electric field:
- Convert the integral equation into a set of algebraic equations
- Solve for induced current density using matrix algebra
- With the current density known, the calculation of the scattered electric field, $\overrightarrow{\mathbf{E}}^{\mathbf{s}}$, is reasonably straightforward and the cross section can be calculated:

$$
\sigma=4 \pi \mathbf{R}^{2} \frac{\left|\mathbf{E}^{S}\right|^{2}}{\left|\mathbf{E}^{\mathbf{I}}\right|^{2}}
$$

## Method of Moments (continued again)

- Break up the target into a set of $\mathbf{N}$ discrete patches
- 7 to 10 patches per wavelength
- Expand the surface current density as a set of known basis functions

$$
\overrightarrow{\mathbf{J}}(\overrightarrow{\mathbf{r}})=\sum_{\mathrm{n}=1}^{\mathrm{N}} \mathbf{I}_{\mathrm{n}} \overrightarrow{\mathbf{B}}_{\mathrm{n}}(\overrightarrow{\mathbf{r}})
$$

- Define the "Magnetic Field Operator", $\mathrm{L}_{\mathbf{H}}(\overrightarrow{\mathbf{J}})$, as

$$
\mathbf{L}_{\mathbf{H}}(\overrightarrow{\mathbf{J}}) \equiv \frac{\overrightarrow{\mathbf{J}}}{2}-\hat{\mathbf{n}} \mathbf{x} \oiint_{\mathbf{S}^{\prime}} \overrightarrow{\mathbf{J}} \mathbf{x} \nabla \psi \mathbf{d} \mathbf{S}^{\prime}
$$

- Insert the series expansion of currents and bringing the sum out of the operator, we get:

$$
\mathbf{L}_{\mathbf{H}}(\vec{J})=\sum_{n=1}^{N} \mathbf{I}_{\mathbf{n}} \mathbf{L}_{\mathbf{H}}\left(\overrightarrow{\mathbf{B}}_{\mathbf{n}}(\overrightarrow{\mathbf{r}})\right)=\hat{\mathbf{n}} \times \overrightarrow{\mathbf{H}}^{1}
$$

## Method of Moments (one last time)

- Multiply by the weighting vector, $\overrightarrow{\mathbf{W}}_{\mathrm{m}}$, and integrating over the surface:

$$
\begin{array}{r}
\oiint_{S}\left[\overrightarrow{\mathbf{W}}(\overrightarrow{\mathbf{r}}) \cdot\left(\hat{\mathbf{n}} \times \overrightarrow{\mathbf{H}}^{\mathrm{I}}\right)\right] \mathrm{dS}-\sum_{\mathrm{n}=1}^{\mathrm{N}} \mathbf{I}_{\mathrm{n}} \mathbf{i} \omega \mu \oiint_{S^{\prime}} \oiint_{\mathrm{S}} \overrightarrow{\mathbf{W}}_{\mathrm{m}} \cdot \mathbf{L}\left(\overrightarrow{\mathbf{B}}_{\mathrm{n}}(\mathbf{r})\right) \mathrm{dS}^{\prime} \mathbf{d S}=\mathbf{0} \\
m=1,2,3, \ldots \mathbf{N}
\end{array}
$$

- Point Testing $\overrightarrow{\mathbf{W}}_{\mathrm{m}}=\delta\left(\overrightarrow{\mathbf{r}}-\overrightarrow{\mathbf{r}}_{\mathrm{m}}\right)$
- Galerkin's Method $\overrightarrow{\mathbf{W}}_{\mathrm{m}}=\overrightarrow{\mathbf{B}}_{\mathrm{m}}(\overrightarrow{\mathbf{r}})$
- This is a set of $\mathbf{N}$ equations in $\mathbf{N}$ unknowns (current coefficients, $\mathrm{I}_{\mathrm{m}}$ ) of the form:

$$
\overrightarrow{\mathbf{Z}} \overrightarrow{\mathbf{I}}=\overrightarrow{\mathbf{V}} \quad \Longrightarrow \overrightarrow{\mathbf{I}}=\overrightarrow{\mathbf{Z}}^{-1} \overline{\mathbf{V}}
$$

- The only difficulty is inversion of a very large matrix


## Monostatic RCS of a Square Plate

- $15 \mathrm{~cm} \times 15 \mathrm{~cm}$ Plate



## Monostatic RCS of a Square Plate

- $15 \mathrm{~cm} \times 15 \mathrm{~cm}$ Plate



## Surface Patch Model of JGAM for Method of Moments RCS Calculation



Photo of JGAM on Pylon


Courtesy of MIT Lincoln Laboratory Used with Permission

IEEE New Hampshire Section

## Summary - Method of Moments

- Method of moments solution is exact
- Patch size must be small enough
- $\mathbf{7}$ to 10 samples per wavelength
- Well suited for small targets at long wavelengths
- Example - Artillery shell at L-Band (23 cm)
- Aircraft size targets result in extremely large matrices to be inverted
- JGAM (~5m length)

1350 unknowns at 1.0 GHz

- Typical Fighter aircraft (~5m length)

A very difficult computation problem at S-Band (10 cm wavelength)

## Comparison of MoM and FD-TD Techniques

- For Single Frequency RCS Predictions (perfect conductors)
- 2-Dimensional Calculation
- 3-Dimensional Calculation

|  | Method of Moments (MoM) | Finite DifferenceTime Domain (FD-TD) |
| :---: | :---: | :---: |
| Method of Calculation | Integral Equation Frequency Domain | Differential Equation Time Domain |
| No. of Unknowns | $N(2-D) \quad \mathrm{N}^{2}(3-\mathrm{D})$ | $\mathrm{N}^{2}$ (2-D) $\quad \mathrm{N}^{3}(3-\mathrm{D})$ |
| Memory Requirement | Matrix Decomposition $N^{3}(2-D) \quad N^{6}(3-D)$ | Time Steps $N^{3}(2-D) \quad N^{4}(3-D)$ |
| Computer Time | $N^{2}(2-D) \quad N^{4}(3-D)$ | $N^{2}(2-D) \quad N^{3}(3-D)$ |
| Accuracy | Exact | Exact |

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| Physical Optics <br> (PO) | Currents Approximated by Tangent <br> Plane Method |
| Geometrical Theory of <br> Diffraction (GTD) | Geometrical Optics with Added Edge <br> Current Contribution |
| Physical Theory of <br> Diffraction (PTD) | Physical Optics with Added Edge <br> Current Contribution |

## Geometrical Optics (GO) - Overview

- Geometrical Optics (GO) is an approximate method for RCS calculation
- Valid in the "optical" region (target size $\gg \lambda$ )
- Based upon ray tracing from the radar to "specular points" on the surface of the target
- "Specular points" are those points, whose normal vector points back to the radar.
- The amount of reflected energy depends on the principal radii of curvature at the surface reflection point
- Geometrical optics (GO) RCS calculations are reasonably accurate to 10 - 15\% for radii of curvature of $2 \lambda$ to $3 \lambda$
- The GO approximation breaks down for flat plates, cylinders and other objects that have infinite radii of curvature; and at edges of these targets



## Geometric Optics



- Power Density Ratio $=\frac{\langle\vec{S}\rangle_{\text {SCAT }}}{\langle\vec{S}\rangle_{\text {INC }}}=\frac{\frac{1}{A_{S}}}{\frac{1}{A_{I}}}=\frac{A_{I}}{A_{S}}=\frac{\frac{\mathbf{a}^{2}}{4} d \Omega}{R^{2} d \Omega}$
- Radar Cross Section of Sphere $=4 \pi R^{2} \frac{\left\langle S_{\text {SCAT }}\right\rangle}{\left\langle S_{I N C}\right\rangle}=4 \pi R^{2} \frac{a^{2}}{4 R^{2}}=\pi \mathbf{a}^{2}$
- Radar Cross Section of an Arbitrary Specular Point $=\pi \rho_{1} \rho_{2}$
- Where radii of curvature at specular point $=\rho_{1}, \rho_{2}$


## Single and Double Reflections



- RCS Calculation for Single Reflection
- Identify all specular points and add contributions
- Phase calculated from distance to and from specular point
- Local radii of curvature used to determine amplitude of backscatter
- RCS Calculation for Double Reflection
- Identify all pairs of specular points
- At each reflection use single reflection methodology to calculate amplitude and phase


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## Physical Optics (PO) Overview

- Physical Optics (PO) is an approximate method for RCS calculation
- Valid in the "optical" region (target size $\gg \lambda$ )
- Method - Physical Optics (PO) calculation
- Modify the Stratton-Chu integral equation form of Maxwell's Equations, assuming that the target is in the far field
- Assume that the total fields, at any point, on the surface of the target are those that would be there if the target were flat

Called "Tangent plane approximation"

- Assume perfectly conducting target
- Resulting equation for the scattered electric field may be readily calculated
- RCS is easily calculated from the scattered electric field
- Physical Optics RCS calculations:
- Give excellent results for normal (or nearly normal) incidence (<30)
- Poor results for shallow grazing angles and near surface edges
e.g. leading and trailing edges of wings or edges of flat plates


## Physical Optics

Tangent Plane Approximation


Infinite Perfectly Conducting Plane (Exact Solution)


Arbitrary Conducting Surface (Approximate Solution)

- For an incident plane wave :

$$
\overrightarrow{\mathbf{J}}_{\mathrm{S}}\left(\overrightarrow{\mathbf{r}}^{\prime}\right)=2 \hat{\mathbf{n}} \times \overrightarrow{\mathbf{H}}_{0} \mathbf{e}^{-\mathrm{i} \mathbf{k} \hat{\mathbf{r}} \cdot \overrightarrow{\mathbf{r}}^{\prime}}
$$

- Substituting this surface current yields (for the monostatic case)

$$
\overrightarrow{\mathbf{E}}_{\mathrm{S}}(\overrightarrow{\mathbf{r}})=-2 i \omega \mu \frac{\mathbf{e}^{i k r}}{4 \pi r} \int \hat{\mathbf{r}} \times \hat{\mathbf{r}} \times\left(\hat{\mathbf{n}} \times \overrightarrow{\mathbf{H}}_{0}\right) \mathbf{e}^{-2 i k \hat{\mathbf{r}} \cdot \overrightarrow{\mathbf{r}}^{\prime}} \mathbf{d} \overrightarrow{\mathbf{r}}^{\prime}
$$

## Normal and Oblique Incidence

- Physical Optics contribution adds constructively (in phase)
- For large plates, the edge contribution is a small part of the total current
- Except near the edges, Physical Optics gives accurate results

- Except near the edges, Physical Optics gives accurate results
- Fresnel Zones of alternating phase caused by phase delay across plate
- In the backscatter direction, the Physical Optics contribution is predominantly cancelled
- The most significant part of total current due to edge effects

Obliquely Incident
Plane Wave

Specular Scattering

## Direction



Fresnel Zones

## Monostatic RCS of a Square Plate

- $15 \mathrm{~cm} \times 15 \mathrm{~cm}$ Plate
10.0 GHz

HH Polarization


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## Geometrical Theory of Diffraction (GTD) Overview

- Geometrical Theory of Diffraction (GTD) a ray tracing method of calculating the diffracted fields at surface edges / discontinuities
- Assumption: When ray impinges on an edge, a cone (see Keller (1957) Cone below) of diffracted rays are generated
- Half angle of cone is equal to the angle, $\beta$, between the edge and the incident ray.

In backscatter case the cone becomes a disk

- Diffracted electric field proportional to "diffraction coefficients", $\mathbf{X}$ and $\mathbf{Y}$ and a "divergence factor, $\Gamma$, and given by:
- Diffraction coefficients

$$
\left|\overrightarrow{\mathbf{E}}_{\mathrm{DIF}}\right|=\frac{\Gamma \mathbf{e}^{\mathrm{iks}} \mathbf{e}^{\mathrm{i} / 4}}{\sin \beta \sqrt{2 \pi \mathrm{ks}}}(\mathbf{X} \mp \mathbf{Y})
$$

-     - when $\overrightarrow{\mathbf{E}}_{\mathrm{I}}$ parallel to edge
-     + when $\overrightarrow{\mathbf{H}}_{\mathrm{I}}$ parallel to edge
- Divergence factor reduces amplitude as rays diverge from scattering point

Edge Diffracted Rays
 and accounts for curves edges

## Geometrical Theory of Diffraction (GTD)

Ray Tracing (With Creeping Waves and Diffraction)


- Advantages
- Easy to Understand
- Multiple Interactions
- Disadvantages
- Implementation difficult for complex targets
- Requires more accurate description than PTD


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## Physical Theory of Diffraction (PTD) Overview



- Approach: Integrate surface current obtained from local tangent plane approximation (plus edge current)
- Advantages: Reduced computational requirements and applicable to arbitrary complex geometries
- Disadvantages: Neglects multiple interactions or shadowing


## Physical Theory of Diffraction (PTD)



- In 1896, Sommerfeld developed a method to find the total scattered field for an the infinite, perfectly conducting wedge.
- In 1957, Ufimtsev obtained the edge current contributions by subtracting the physical optics contributions from the total scattered field.
- The current for finite length structures may be obtained by truncating the edge current from that of the infinite structure


## Normal and Oblique Diffraction



- Constructive addition from edge current contribution along entire edge results in strong perpendicular backscatter
- Small contribution from corner edge current
- Perpendicular to edge, scattering is strong in all directions
- Edge current contribution interferes destructively in direction of backscatter
- For near grazing angles, corner current may be significant
- Strong scattering along "Keller Cone"


## Trailing / Leading Edge Diffraction



Field

- Negligible scattering at front edge - Electric field normal and continuous
- Traveling waves; above and below plate develop a relative phase delay.
- Required continuity of electric field at back edge causes induced edge current, and thus a diffracted electric field.

Leading Edge Diffraction


- Tangential component of electric field equals zero along the conductor.
- Diffracted electric field is produced by current induced to cancel incident electric field.
- No diffraction at back edge because electric field is close to zero.


## FD-TD Simulation of Scattering by Strip

- Gaussian pulse plane wave incidence

Case 2

- E-field polarization ( $E_{y}$ plotted)
- Phenomena: leading edge diffraction



## FD-TD Simulation of Scattering by Strip

## Case 2

## FD-TD Simulation of Scattering by Strip

- Gaussian pulse plane wave incidence


## Case 3

- H-field polarization ( $\mathrm{H}_{\mathrm{y}}$ plotted)
- Phenomena: trailing edge diffraction



## FD-TD Simulation of Scattering by Strip

## Case 3

## Monostatic RCS of a Square Plate

- $15 \mathrm{~cm} \times 15 \mathrm{~cm}$ Plate
10.0 GHz

HH Polarization


## Measured and Predicted RCS of JGAM

Courtesy of MIT Lincoln Laboratory Used with permission


## Radar Cross Section Calculation Methods

- Introduction
- A look at the few simple problems
- RCS prediction
- Exact Techniques

Finite Difference- Finite Time Technique (FD-FT)
Method of Moments (MOM)

- Approximate Techniques

Geometrical Optics (GO)
Physical Optics (PO)
Geometrical Theory of Diffraction (GTD)
Physical Theory of Diffraction (PTD)
$\longrightarrow$ - Comparison of different methodologies

## RCS Prediction Techniques Family Tree

## Exact Techniques

- Limited Geometry


- Limited Phenomena
- Computationally Speedy

-Computationally Slow -All Geometries

Geometrical Optics (GO)
Geometrical Theory
of Diffraction (GTD)
Universal Theory
of Diffraction (UTD)
Shooting and Bouncing

Method of Moments (MoM) Other Integral Techniques

Hybrid Methods

Rays (SBR)

## Differential <br> Equation <br> Solutions

Finite Element
Finite Difference-Time Domain (FT-TD)
Finite Difference-Frequency Domain (FD-FD)

## Comparison of Different RCS Calculation Techniques

|  | Methods of Calculation |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | FT-TD | MOM | GO - GTD | PO-PTD |
| Calculation Of Current | Exact Solve Partial Differential Equation | Exact <br> (Solve Integral Equation) | Specular Point Reflections (Edge Currents) | Tangent Plane Approximation <br> (Edge Currents) |
| Physical Phenomena Considered | All | All | Ray Tracing | Reflections (Single \& Double) Diffraction |
| Main Computational Requirement | Time Stepping | Matrix Inversion | Multiple Reflection Diffraction | Surface Integration Shadowing |
| Advantages | Exact <br> Visualization Aids Physical Insight | Exact | - Simple Formulation - Good Insight into Physical Phenomena | Easiest Computationally - Good Insight into Physical Phenomena |
| Limitations And/or Disadvantages | - Low Frequency Only - Complex <br> Geometries Difficult - Single Incident Angle | - Low Frequency Only <br> - Formulation Difficult (Materials) <br> - Single Frequency | - High Frequency Only <br> - Canonical <br> Geometries Only <br> - Caustics | - High Frequency Only <br> - Many Phenomena Neglected |

## Corner Reflectors

- Give a large reflection, $\sigma$, over a wide range of angles
- Used as test targets and for radar calibration

Sailboat Based
Circular Trihedral Corner Reflector

- Different shapes
- Dihedral
- Trihedral

Square, triangular, and circular


Courtesy of dalydaly
RCS of Dihedral Corner Reflector
(Broadside Incidence)

$$
\begin{gathered}
\sigma=\frac{4 \pi \mathrm{~A}_{\mathrm{EF}}^{2}}{\lambda^{2}} \\
\mathrm{~A}_{\mathrm{EF}}=\begin{array}{l}
\text { Area of projected aperture } \\
\text { On the incident ray }
\end{array}
\end{gathered}
$$

Ray Trace for a Dihedral Corner Reflector (Side view)

## Summary

- Target RCS depends on its characteristics and the radar parameters
- Target : size, shape, material, orientation
- Radar : frequency, polarization, range, viewing angles, etc
- The target RCS is due to many different scattering centers
- Structural, Propulsion, and Avionics
- Many RCS calculation tools are available
- Take into account the many different electromagnetic scattering mechanisms present
- Measurements and predictions are synergistic
- Measurements anchor predictions
- Predictions validate measurements


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## Homework Problems

- From Skolnik (Reference 2)
- Problems 2-10, 2-11, 2-12, and 2-13
- From Levanon (Reference 6)
- Problems 2-1 and 2-5
- For an ellipsoid of revolution, (semi major axis, a , aligned with the x-axis, semi minor axis, $b$, aligned with the $y$ axis, and axis of rotation is the x-axis; what are the radar cross sections (far field) looking down the $x, y$, and $z$ axes, if the radar has wavelength $\lambda$ and $a \gg \lambda$ and $b \gg \lambda$ ?
- Extra credit: Solve the last problem assuming $\mathbf{a} \ll \lambda$ and $\mathbf{b}$ $\ll \lambda$.

